

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

$$\frac{d}{dx}(e^{kx}) = ke^{kx}$$

$$\frac{d}{dx}(\sin x) = \cos x$$

$$\frac{d}{dx}(\cos x) = -\sin x$$

$$\frac{d}{dx}(\tan x) = \sec^2 x$$

$$\frac{d}{dx}(\cot x) = -\csc^2 x$$

$$\frac{d}{dx}(\csc x) = -\csc x \cot x$$

$$\frac{d}{dx}(\sec x) = \sec x \tan x$$

$$\frac{d}{dx}(fg) = f'g + fg'$$

$$\frac{d}{dx}\left(\frac{f}{g}\right) = \frac{f'g - fg'}{g^2}$$

day 32

HW due tomorrow

3.6 / 11-12, 19, 27-30

3.7 / 10-12, 19-22, 35-36

day 32

$\frac{d}{dx}(x^n) = nx^{n-1}$ 
 $\frac{d}{dx}(fg) = f'g + fg'$ 
 $\frac{d}{dx}\left(\frac{f}{g}\right) = \frac{f'g - fg'}{g^2}$

$\frac{d}{dx}(e^{kx}) = ke^{kx}$   
 $\frac{d}{dx}(\sin x) = \cos x$   
 $\frac{d}{dx}(\cos x) = -\sin x$   
 $\frac{d}{dx}(\tan x) = \sec^2 x$   
 $\frac{d}{dx}(\cot x) = -\csc^2 x$   
 $\frac{d}{dx}(\csc x) = -\csc x \cot x$   
 $\frac{d}{dx}(\sec x) = \sec x \tan x$

3.6/17) 1995 ( $t=0$ )  $\rightarrow$  2005 ( $t=10$ )

$p(t) = -0.27t^2 + 101t + 7055$

a) avg growth:  $\frac{p(10) - p(0)}{10 - 0} =$

$= \frac{-27 + 1010 + 7055 - 7055}{10} = 98.3$   
thousand ppl  
yr

b) what was the growth rate at  $t=2$ ?

$p'(t) = -0.54t + 101$   
 $p'(2) = 99.2$   
 $p'(10) = 95.6$  /tho ppl/yr

$\frac{d}{dx}(x^n) = nx^{n-1}$   
 $\frac{d}{dx}(e^{kx}) = k e^{kx}$   
 $\frac{d}{dx}(\sin x) = \cos x$   
 $\frac{d}{dx}(\cos x) = -\sin x$   
 $\frac{d}{dx}(\tan x) = \sec^2 x$   
 $\frac{d}{dx}(\cot x) = -\csc^2 x$   
 $\frac{d}{dx}(\sec x) = \sec x \tan x$   
 $\frac{d}{dx}(\csc x) = -\csc x \cot x$

$\frac{d}{dx}(fg) = f'g + fg'$   
 $\frac{d}{dx}\left(\frac{f}{g}\right) = \frac{f'g - fg'}{g^2}$

day 32

3.6/23

$f(t) = h_1(t) = -16t^2 + 32t + 48$

$g(t) = h_2(t) = -16t^2 + 16t$

find  $V_0$  so max height is same

max height of  $f(t)$ : when  $v(t) = 0$   
 [use calc II]

$f'(t) = -32t + 32 \Rightarrow t = 1$   
 $f(1) = 64 \text{ ft}$

precalc way: find vertex [first find axis of symmetry]

$f(t) = -16t^2 + 32t$   
 $= -16t(t-2)$   
 x-int at  $t=0, t=2$   
 axis of sym =  $\frac{0+2}{2} = 1$

want max height of  $-16t^2 + 16t = 64$   
 at  $t=1$   
 $-16 + V_0 = 64$   
 $V_0 = 80 \text{ ft/sec}$

$g(t) = -16t^2 + V_0 t$   
 $g'(t) = -32t + V_0$   
 $0 = -32t + V_0$   
 $32t = V_0$   
 $t = \frac{V_0}{32} \Rightarrow g\left(\frac{V_0}{32}\right) = -16\left(\frac{V_0}{32}\right)^2 + V_0\left(\frac{V_0}{32}\right)$

$g\left(\frac{V_0}{32}\right) = \frac{-16}{32 \cdot 32} V_0^2 + \frac{1}{32} V_0^2 = V_0^2 \left[ \frac{-1}{64} + \frac{1}{32} \right] = \frac{1}{64} V_0^2$

$64 = \frac{1}{64} V_0^2 \Rightarrow (64)^2 = V_0^2$   
 so  $(V_0 = 64)$  to make height 64 ft

day 32

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

$$\frac{d}{dx}(fg) = f'g + fg'$$

$$\frac{d}{dx}\left(\frac{f}{g}\right) = \frac{f'g - fg'}{g^2}$$

$$\frac{d}{dx}(e^{kx}) = ke^{kx}$$

3.6/10)  $f(t) = -t^2 + 4t - 3; t \in [0, 5]$

$$\frac{d}{dx}(\sin x) = \cos x$$

$$\frac{d}{dx}(\cos x) = -\sin x$$

$$\frac{d}{dx}(\tan x) = \sec^2 x$$

$$\frac{d}{dx}(\cot x) = -\csc^2 x$$

$$\frac{d}{dx}(\csc x) = -\csc x \cot x$$

$$\frac{d}{dx}(\sec x) = \sec x \tan x$$

a.  $\cap$

b.  $v(t) = f'(t) = -2t + 4$

c.  $v(1) = -2(1) + 4 = 2$

$a(1) = -2$

d)  $a(t) = -2$   
because  $a(t) = -2$

e) speed increasing.

sign of  $v(t)$   $++++|-----$   
sign of  $a(t)$   $-----|-----$

speeding up on  $(2, \infty)$



$\frac{d}{dx}(x^n) = nx^{n-1}$ 
 $\frac{d}{dx}(fg) = f'g + fg'$ 
 $\frac{d}{dx}\left(\frac{f}{g}\right) = \frac{f'g - fg'}{g^2}$ 
 day 32

$\frac{d}{dx}(e^{kx}) = ke^{kx}$

$\frac{d}{dx}(\sin x) = \cos x$

$\frac{d}{dx}(\cos x) = -\sin x$


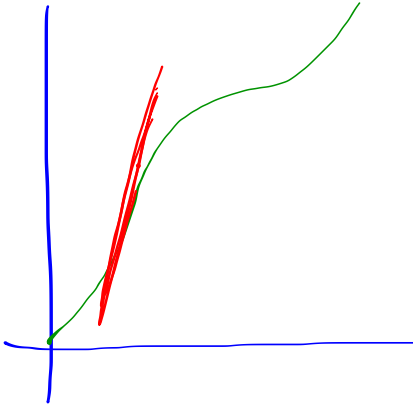
$\frac{d}{dx}(\tan x) = \sec^2 x$

$\frac{d}{dx}(\cot x) = -\csc^2 x$

$\frac{d}{dx}(\csc x) = -\csc x \cot x$

$\frac{d}{dx}(\sec x) = \sec x \tan x$

3.6/24

day 32

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

$$\frac{d}{dx}(fg) = f'g + fg'$$

$$\frac{d}{dx}\left(\frac{f}{g}\right) = \frac{f'g - fg'}{g^2}$$

$$\frac{d}{dx}(e^{kx}) = ke^{kx}$$

3.7/6)  $Q(x) = \cos^4(x^2+1) = [\cos(x^2+1)]^4$

$$\frac{d}{dx}(\sin x) = \cos x$$

$$\frac{d}{dx}(\cos x) = -\sin x$$

$$\frac{d}{dx}(\tan x) = \sec^2 x$$

$$\frac{d}{dx}(\cot x) = -\csc^2 x$$

$$\frac{d}{dx}(\csc x) = -\csc x \cot x$$

$$\frac{d}{dx}(\sec x) = \sec x \tan x$$

$$x \xrightarrow{h(x)} (x^2+1) \xrightarrow{g(x)} \cos(x^2+1)$$

$$f(x) = x^4$$

$$f'(x) = 4x^3$$

$$g(x) = \cos(x)$$

$$g'(x) = -\sin(x)$$

$$h(x) = x^2+1$$

$$h'(x) = 2x$$

$$\begin{matrix} \searrow f(x) \\ [\cos(x^2+1)]^4 \end{matrix}$$

$$\frac{d}{dx}[f(g(h(x)))] = f'(g(h(x))) \cdot \frac{d}{dx}(g(h(x)))$$

$$= f'(g(h(x))) \cdot g'(h(x)) \cdot h'(x)$$

$$= 4(\cos(x^2+1))^3 \cdot (-\sin(x^2+1)) \cdot (2x)$$